

CONTRACTIVE MAPPINGS AND COMMON FIXED POINT THEOREMS IN INTUITIONISTIC FUZZY METRIC SPACES

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ABSTRACT. This paper deals with some issues of common fixed point theory involving two different types of intuitionistic fuzzy contractive mappings. Intuitionistic fuzzy Jungck's common fixed point theorem (see, [1]) with respect to contraction defined in [8] and intuitionistic fuzzy Pant's common fixed point theorem (see, [2]) for ψ - ϕ weakly commuting mappings are proved.

Key Words: Intuitionistic fuzzy metric space, contractive mappings, commutative mappings, weakly commuting mappings, common fixed point.

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1. INTRODUCTION

The concept of intuitionistic fuzzy set as a generalization of fuzzy set [13] was introduced by Atansov [12]. George and Veeramani [5] have modified the definition of fuzzy metric which is introduced by Kramosil and Michalek [10].

Sessa [3] introduce a generalization of commutativity called weak commutativity. Further, Jungck [1] introduced more generalized commutativity which is called compatibility in metric space. He also proved

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common fixed point theorems. Pant [2] proved common fixed point theorems for non-commuting mappings.

In this paper, we prove the intuitionistic fuzzy version of two common fixed point theorems, namely; Jungck's and Pant's theorems for two generalized contractive mappings.

2. PRELIMINARIES

We quote some definitions and statements of a few theorems which will be needed in the sequel.

Definition 2.1. [11] A binary operation $*$: $[0, 1] \times [0, 1] \rightarrow [0, 1]$ is continuous t -norm if $*$, satisfies the following conditions:

- (i) $*$ is commutative and associative,
- (ii) $*$ is continuous,
- (iii) $a * 1 = a$ for every $a \in [0, 1]$,
- (iv) $a * b \leq c * d$ whenever $a \leq c$, $b \leq d$ and $a, b, c, d \in [0, 1]$.

A few examples of continuous t -norms are $a * b = ab$, $a * b = \min\{a, b\}$, $a * b = \max\{a + b - 1, 0\}$.

Definition 2.2. [11]. A binary operation \diamond : $[0, 1] \times [0, 1] \rightarrow [0, 1]$, is continuous t -conorm if \diamond satisfies the following conditions:

- (i) \diamond is commutative and associative,
- (ii) \diamond is continuous,
- (iii) $a \diamond 0 = a$ for every $a \in [0, 1]$,
- (iv) $a \diamond b \leq c \diamond d$ whenever $a \leq c$, $b \leq d$ and $a, b, c, d \in [0, 1]$.

A few examples of continuous t -conorms are $a \diamond b = a + b - ab$, $a \diamond b = \max\{a, b\}$, $a \diamond b = \min\{a + b, 1\}$.

Definition 2.3. [4] A 5-tuple $(X, \mu, \nu, *, \diamond)$ is said to be an intuitionistic fuzzy metric space if X is an arbitrary set, $*$ is a continuous t -norm, \diamond is a continuous t -conorm, μ and ν are fuzzy sets on $X^2 \times (0, \infty)$ and μ denotes the degree of nearness, ν denotes the degree of non-nearness between x and y relative to t satisfying the following conditions: for all

- $x, y, z \in X, s, t > 0,$
- (i) $\mu(x, y, t) + \nu(x, y, t) \leq 1$
 - (ii) $\mu(x, y, t) > 0;$
 - (iii) $\mu(x, y, t) = 1$ if and only if $x = y;$
 - (iv) $\mu(x, y, t) = \mu(y, x, t);$
 - (v) $\mu(x, z, t + s) \geq \mu(x, y, t) * \mu(y, z, s);$
 - (vi) $\mu(x, y, \cdot) : (0, \infty) \rightarrow (0, 1]$ is continuous;
 - (vii) $\nu(x, y, t) > 0;$
 - (viii) $\nu(x, y, t) = 0$ if and only if $x = y;$
 - (ix) $\nu(x, y, t) = \nu(y, x, t);$
 - (x) $\nu(x, z, t + s) \leq \nu(x, y, t) \diamond \nu(y, z, s);$
 - (xi) $\nu(x, y, \cdot) : (0, \infty) \rightarrow (0, 1]$ is continuous.

Definition 2.4. [7] Let Ψ be the class of all mappings $\psi : [0, 1] \rightarrow [0, 1]$ such that ψ is continuous, non-increasing and $\psi(t) < t, \forall t \in (0, 1)$. Let Φ be the class of all mappings $\phi : [0, 1] \rightarrow [0, 1]$ such that ϕ is continuous, non-decreasing and $\phi(t) > t, \forall t \in (0, 1)$. Let $(X, \mu, \nu, *, \diamond)$ be an intuitionistic fuzzy metric space and $\psi \in \Psi$ and $\phi \in \Phi$. A mapping $f : X \rightarrow X$ is called an intuitionistic fuzzy ψ - ϕ -contractive mapping if the following implications hold:

$$\begin{aligned} \mu(x, y, t) > 0 &\Rightarrow \psi(\mu(f(x), f(y), t)) \geq \mu(x, y, t) \\ \nu(x, y, t) < 1 &\Rightarrow \phi(\nu(f(x), f(y), t)) \leq \nu(x, y, t). \end{aligned}$$

Definition 2.5. [8] Let (X, A) be an intuitionistic fuzzy metric space and $T : X \rightarrow X$. T is said to be TS -intuitionistic fuzzy contractive mapping if the following conditions hold for $k \in (0, 1)$

$$k \mu(T(x), T(y), t) \geq \mu(x, y, t)$$

and

$$\frac{1}{k} \nu(T(x), T(y), t) \leq \nu(x, y, t), \quad t > 0.$$

Definition 2.6. [9] Let f and g be two mappings from a metric space (X, d) into itself. The mappings f and g are said to be weakly commuting

if

$$d(f(g(x)), g(f(x))) \leq d(f(x), g(x)), \forall x \in X.$$

3. COMMON FIXED POINT THEOREMS FOR COMMUTING MAPPINGS

Theorem 3.1. *Let $(X, \mu, \nu, *, \diamond)$ be a complete intuitionistic fuzzy metric space and $f, g : X \rightarrow X$ be such that*

(i) $g(X) \subseteq f(X)$,

(ii) f is continuous on X ,

(iii) there exists $k \in (0, 1)$ such that for all $x, y \in X$ and $t > 0$,

$$\begin{aligned} k \mu(g(x), g(y), t) &\geq \mu(f(x), f(y), t) \\ \frac{1}{k} \nu(g(x), g(y), t) &\leq \nu(f(x), f(y), t), \quad t > 0. \end{aligned}$$

Then f and g have a unique common fixed point in X provided f, g commute on X .

Proof. Let $x_0 \in X$. By (i), we can find $x_1 \in X$ such that $f(x_1) = g(x_0)$. So, we can define a sequence $\{x_n\}_n$ in X such that $f(x_n) = g(x_{n-1})$. Now,

$$\begin{aligned} k^n \mu(f(x_n), f(x_{n+1}), t) &= k^n \mu(g(x_{n-1}), g(x_n), t) \\ &\geq k^{n-1} (k \mu(g(x_{n-1}), g(x_n), t)) \\ &= k^{n-1} \mu(f(x_{n-1}), f(x_n), t) \\ &= k^{n-2} (k \mu(g(x_{n-2}), g(x_{n-1}), t)) \\ &\geq k^{n-2} \mu(f(x_{n-2}), f(x_{n-1}), t) \\ &\geq \cdots \geq \mu(f(x_0), f(x_1), t) \end{aligned}$$

and

$$\frac{1}{k^n} \nu(f(x_n), f(x_{n+1}), t) \leq \nu(f(x_0), f(x_1), t).$$

Therefore

$$\begin{aligned} &\mu(f(x_n), f(x_{n+p}), t) \\ &\geq \mu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) * \mu\left(f(x_{n+1}), f(x_{n+2}), \frac{t}{p}\right) * \end{aligned}$$

$$\begin{aligned}
& \cdots * \mu \left(f(x_{n+p-1}), f(x_{n+p}), \frac{t}{p} \right) \\
= & \frac{1}{k^n} k^n \mu \left(f(x_n), f(x_{n+1}), \frac{t}{p} \right) * \frac{1}{k^{n+1}} k^{n+1} \mu \left(f(x_{n+1}), f(x_{n+2}), \frac{t}{p} \right) * \\
& \cdots * \frac{1}{k^{n+p-1}} k^{n+p-1} \mu \left(f(x_{n+p-1}), f(x_{n+p}), \frac{t}{p} \right) \\
= & \frac{1}{k^n} \mu (f(x_0), f(x_1), t_1) * \frac{1}{k^{n+1}} \mu (f(x_0), f(x_1), t_1) * \\
& \cdots * \frac{1}{k^{n+p-1}} \mu (f(x_0), f(x_1), t_1), \text{ where } t_1 = \frac{t}{p}. \\
\geq & \frac{1}{k^n} \mu (f(x_0), f(x_1), t_1), \text{ since } a \geq c \Rightarrow a * c \geq c * c \geq c.
\end{aligned}$$

Thus we have

$$\mu (f(x_n), f(x_{n+p}), t) \geq \frac{1}{k^n} \mu (f(x_0), f(x_1), t_1).$$

Similarly we have

$$\nu (f(x_n), f(x_{n+p}), t) \geq k^n \nu (f(x_0), f(x_1), t_1).$$

Now

$$\begin{aligned}
\lim_{n \rightarrow \infty} \mu (f(x_n), f(x_{n+p}), t) & \geq \lim_{n \rightarrow \infty} \frac{1}{k^n} \mu (f(x_0), f(x_1), t_1) \geq 1. \\
\lim_{n \rightarrow \infty} \nu (f(x_n), f(x_{n+p}), t) & \leq \lim_{n \rightarrow \infty} k^n \nu (f(x_0), f(x_1), t_1) \leq 0.
\end{aligned}$$

Therefore

$$\lim_{n \rightarrow \infty} \mu (f(x_n), f(x_{n+p}), t) = 1, \quad \lim_{n \rightarrow \infty} \nu (f(x_n), f(x_{n+p}), t) = 0.$$

$$\Rightarrow \{f(x_n)\}_n \text{ is a sequence in } (X, \mu, \nu, *, \diamond).$$

$$\Rightarrow \exists y \in X \text{ such that } f(x_n) \rightarrow y \text{ as } n \rightarrow \infty \text{ in } (X, \mu, \nu, *, \diamond).$$

Since $g(x_{n+1}) = f(x_n)$, it follows that $g(x_n) \rightarrow y$ as $n \rightarrow \infty$ in $(X, \mu, \nu, *, \diamond)$.

The continuity of f implies the continuity of g by (iii). Therefore, $\{g(f(x_n))\}_n$ converges to $g(y)$ in $(X, \mu, \nu, *, \diamond)$. However, since f and g commute on X , $g(f(x_n))$ and $f(g(x_n))$ are so and $f(g(x_n)) \rightarrow f(y)$ as $n \rightarrow \infty$. Since the limits are unique, $f(y) = g(y)$, which implies that $f(f(y)) = f(g(y))$.

$$\text{Now } \mu(g(y), g(g(y)), t) = \frac{1}{k} k \mu(g(y), g(g(y)), t) \geq \frac{1}{k} \mu(f(y), f(g(y)), t) =$$

$\frac{1}{k} \mu(f(y), g(f(y)), t) = \frac{1}{k} \mu(g(y), g(g(y)), t) \geq \dots \geq \frac{1}{k^n} \mu(g(y), g(g(y)), t)$.
 Similarly, $\mu(g(y), g(g(y)), t) \leq k^n \mu(g(y), g(g(y)), t)$.

Therefore, $g(y) = g(g(y))$ and hence $g(y) = g(g(y)) = g(f(y)) = f(g(y)) \Rightarrow g(y)$ is a common fixed point of f and g .

If y and z are two common fixed points of f and g then

$$\begin{aligned}
 1 &\geq \mu(y, z, t) = \mu(g(y), g(z), t) = \frac{1}{k} k \mu(g(y), g(z), t) \geq \frac{1}{k} \mu(f(y), f(z), t) = \\
 \mu(y, z, t) &= \frac{1}{k^2} k \mu(g(y), g(z), t) \geq \frac{1}{k^2} \mu(f(y), f(z), t) = \dots \geq \frac{1}{k^n} \mu(y, z, t) \geq \\
 &1.
 \end{aligned}$$

Similarly, $0 \leq \nu(y, z, t) \leq 0$. Therefore, $\mu(y, z, t) = 1$, $\nu(y, z, t) = 0$.
 Hence $y = z$. This completes the proof. \square

4. COMMON FIXED POINT THEOREMS FOR Ψ - Φ -WEAKLY COMMUTING MAPPINGS

Definition 4.1. Let f and g be self mappings of an intuitionistic fuzzy metric space $(X, \mu, \nu, *, \diamond)$. The mappings f and g are said to be Ψ - Φ -weakly commuting if

$$\begin{aligned}
 \psi(\mu(f(g(x)), g(f(x)), t)) &\geq \mu(f(x), g(x), t), \\
 \phi(\nu(f(g(x)), g(f(x)), t)) &\leq \nu(f(x), g(x), t).
 \end{aligned}$$

Theorem 4.2. Let $(X, \mu, \nu, *, \diamond)$ be a complete intuitionistic fuzzy metric space and f, g be intuitionistic fuzzy Ψ - Φ -weakly commuting self mappings of X satisfying the following conditions

- (i) $f(X) \subset g(X)$,
- (ii) f or g is continuous,
- (iii) for all $x, y \in X$ and $0 < t < 1$

$$\begin{aligned}
 \mu(f(x), f(y), t) &\geq \phi(\mu(g(x), g(y), t)), \\
 \nu(f(x), f(y), t) &\leq \psi(\nu(g(x), g(y), t)).
 \end{aligned}$$

(iv) $\lim_{n \rightarrow \infty} x_n = x$ and $\lim_{n \rightarrow \infty} y_n = y$ implies $\lim_{n \rightarrow \infty} \mu(x_n, y_n, t) = \mu(x, y, t)$
 and $\lim_{n \rightarrow \infty} \nu(x_n, y_n, t) = \nu(x, y, t)$ then f and g have unique common fixed point in X .

Proof. Let $x_0 \in X$. Choose a point x_1 in X such that $f(x_0) = g(x_1)$. In general, we can choose x_{n+1} such that $f(x_n) = g(x_{n+1})$ for all $n \geq 0$. Then for all $t > 0$:

$$\begin{aligned} \mu(f(x_n), f(x_{n+1}, t)) &\geq \phi(\mu(g(x_n), g(x_{n+1}, t))) = \phi(\mu(f(x_{n-1}), f(x_n, t))) \\ &> \mu(f(x_n), f(x_{n+1}, t)), \\ \nu(f(x_n), f(x_{n+1}, t)) &\leq \psi(\nu(g(x_n), g(x_{n+1}, t))) = \psi(\nu(f(x_{n-1}), f(x_n, t))) \\ &< \nu(f(x_n), f(x_{n+1}, t)). \end{aligned}$$

Thus $\{\mu(f(x_n), f(x_{n+1}, t))\}_n$ is an increasing sequence and $\{\nu(f(x_n), f(x_{n+1}, t))\}_n$ is a decreasing sequence of positive real numbers in $[0, 1]$. Therefore they converges to the limits $l \leq 1$ and $l' \geq 0$ respectively.

Now we claim that $l = 1$ and $l' = 0$. For $l < 1$, we have $l \geq \phi(l) > l$, a contradiction. So, $l = 1$. Similarly, for $l' > 0$ we have $l' \leq \psi(l') < l'$, a contradiction. So, $l' = 0$.

Now for any positive integer p and $t > 0$, we have

$$\begin{aligned} \mu(f(x_n), f(x_{n+p}, t)) &\geq \mu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) * \mu\left(f(x_{n+1}), f(x_{n+2}), \frac{t}{p}\right) * \\ &\quad \cdots * \mu\left(f(x_{n+p-1}), f(x_{n+p}), \frac{t}{p}\right) \\ &\geq \mu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) * \mu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) * \\ &\quad \cdots * \mu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) \end{aligned}$$

and

$$\begin{aligned} \nu(f(x_n), f(x_{n+p}, t)) &\leq \nu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) \diamond \nu\left(f(x_{n+1}), f(x_{n+2}), \frac{t}{p}\right) \diamond \\ &\quad \cdots \diamond \nu\left(f(x_{n+p-1}), f(x_{n+p}), \frac{t}{p}\right) \\ &\leq \nu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) \diamond \nu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right) \diamond \\ &\quad \cdots \diamond \nu\left(f(x_n), f(x_{n+1}), \frac{t}{p}\right). \end{aligned}$$

Since we have

$$\lim_{n \rightarrow \infty} \mu \left(f(x_n), f(x_{n+1}), \frac{t}{p} \right) = 1, \quad \lim_{n \rightarrow \infty} \nu \left(f(x_n), f(x_{n+1}), \frac{t}{p} \right) = 0.$$

It follows that

$$\lim_{n \rightarrow \infty} \mu (f(x_n), f(x_{n+p}), t) \geq 1 * 1 * \dots * 1 \geq 1,$$

$$\lim_{n \rightarrow \infty} \nu (f(x_n), f(x_{n+p}), t) \leq 0 \diamond 0 \diamond \dots \diamond 0 \leq 0.$$

Therefore, $\lim_{n \rightarrow \infty} \mu (f(x_n), f(x_{n+p}), t) = 1$ and $\lim_{n \rightarrow \infty} \nu (f(x_n), f(x_{n+p}), t) = 0$. Thus, $\{f(x_n)\}_n$ is a Cauchy sequence and since X is complete, $\{f(x_n)\}_n$ converges to a point $z \in X$. Also, $\{g(x_n)\}_n$ converges to z .

Suppose that, by (ii), f is uniformly intuitionistic fuzzy continuous. Then $\lim_{n \rightarrow \infty} f(f(x_n)) = f(z)$ and $\lim_{n \rightarrow \infty} f(g(x_n)) = f(z)$. Further, since f and g are ψ - ϕ weakly commuting, we have

$$\psi (\mu (f(g(x)), g(f(x))), t) \geq \mu (f(x), g(x), t),$$

$$\phi (\nu (f(g(x)), g(f(x))), t) \leq \nu (f(x), g(x), t).$$

Letting $n \rightarrow \infty$ in the inequality and by (iv), we have $\lim_{n \rightarrow \infty} g(f(x_n)) = f(z)$.

Now we prove that $z = f(z)$. If possible let $z \neq f(z)$. Then there exists $t > 0$ such that $\mu(z, f(z), t) < 1$ and $\nu(z, f(z), t) > 0$. From (iii) we have

$$\mu (f(x_n), f(f(x_n))), t \geq \phi (\mu (g(x_n), g(f(x_n))), t),$$

$$\nu (f(x_n), f(f(x_n))), t \geq \psi (\nu (g(x_n), g(f(x_n))), t).$$

Taking limit as $n \rightarrow \infty$ we have

$$\mu (z, f(z), t) \geq \phi (\mu (z, f(z), t)) > \mu (z, f(z), t),$$

$$\nu (z, f(z), t) \leq \psi (\nu (z, f(z), t)) < \nu (z, f(z), t),$$

which are contradictions. Therefore $z = f(z)$.

By (i), we can find a point $z_1 \in X$ such that $z = f(z) = g(z_1)$. Now, it follows that

$$\mu (f(f(x_n)), f(z_1), t) \geq \phi (\mu (g(f(x_n)), g(z_1), t)),$$

$$\nu(f(f(x_n)), f(z_1), t) \leq \psi(\nu(g(f(x_n)), g(z_1), t)).$$

Taking limit as $n \rightarrow \infty$ we have

$$\mu(f(z), f(z_1), t) \geq \phi(\mu(f(z), g(z_1), t)) = 1,$$

$$\nu(f(z), f(z_1), t) \leq \psi(\nu(f(z), g(z_1), t)) = 0,$$

since $\phi(1) = 1$ and $\psi(0) = 0$. This implies that $f(z) = f(z_1)$ i.e., $z = f(z) = f(z_1) = g(z_1)$. Also for any $t > 0$

$$\psi(\mu(f(z), g(z), t)) = \psi(\mu(f(g(z_1)), g(f(z_1)), t)) \geq \mu(f(z_1), g(z_1), t) = 1.$$

Therefore, $\psi(\mu(f(z), g(z), t)) = 1$ and hence $\mu(f(z), g(z), t) = 1$.

$$\phi(\nu(f(z), g(z), t)) = \phi(\nu(f(g(z_1)), g(f(z_1)), t)) \leq \mu(f(z_1), g(z_1), t) = 0.$$

Therefore, $\phi(\nu(f(z), g(z), t)) = 0$ and hence $\nu(f(z), g(z), t) = 0$.

Which again implies that $f(z) = g(z)$. Therefore z is a common fixed point of f and g .

If x, y are fixed points of f then

$$\mu(f(x), f(y), t) = \mu(x, y, t) \leq \psi(\mu(f(x), f(y), t))$$

and

$$\nu(f(x), f(y), t) = \nu(x, y, t) \geq \phi(\nu(f(x), f(y), t)), \forall t > 0.$$

If $x \neq y$ then $\mu(x, y, s) < 1$ and $\nu(x, y, s) > 0$ for some $s > 0$ i.e., $0 < \mu(x, y, s) < 1$ and $0 < \nu(x, y, s) < 1$ hold, implying

$$\mu(f(x), f(y), s) \leq \psi(\mu(f(x), f(y), s)) < \mu(f(x), f(y), s)$$

and

$$\nu(f(x), f(y), s) \geq \phi(\nu(f(x), f(y), s)) > \nu(f(x), f(y), s)$$

which are contradictions. Thus $x = y$. This completes the proof. \square

Example 4.3. Let $(X, \|\cdot\|)$ be a normed linear space and consider $a * b = ab$ and $a \diamond b = \min\{a+b, 1\}$. Define $\mu, \nu : V \times V \times \mathbb{R} \rightarrow [0, 1]$ by

$$\mu(x, y, t) = \frac{t}{t + \|x - y\|}, \quad \nu(x, y, t) = \frac{\|x - y\|}{t + \|x - y\|}$$

Then clearly $(V, \mu, \nu, *, \diamond)$ is an intuitionistic fuzzy metric space.

Define two self mappings f and g on X by

$$f(x) = 1 \text{ and } g(x) = \begin{cases} 1, & \text{if } x \text{ is a rational number} \\ 0, & \text{if } x \text{ is an irrational number.} \end{cases}$$

Then $f(X) \subset g(X)$, f is continuous and g is discontinuous.

Define $\psi(t) = t^2$ and $\phi(t) = \sqrt{t}$, for $t \in (0, 1)$. Then $\psi(t) < t$ and $\phi(t) > t$ and for all $x, y \in X$

$$\mu(f(x), f(y), t) \geq \phi(\mu(g(x), g(y), t)),$$

$$\nu(f(x), f(y), t) \leq \psi(\nu(g(x), g(y), t)).$$

Also, f and g are ψ - ϕ weakly commuting. Hence 1 is a common fixed point of f and g .

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